

# Purley C of E Primary School Calculation Policy

March 2021

# Helping you to help your child: Calculation methods

#### Introduction:

The aim of this policy is to show the steps that are covered when teaching the four operations of addition, subtraction, multiplication and division. This updated version of the policy also includes pictorial representations of the equipment that might be used to show the step visually - a key part of how the operations are taught in our school.

Children are introduced to the processes of calculation through practical, oral and mental activities. As they begin to understand the underlying ideas, they develop ways of recording to support their thinking and calculation methods, so that they develop both **conceptual understanding** and **fluency** in the basics of mathematics. Whilst interpreting signs and symbols involved with calculation, orally in the first instance, children use both hands-on items as well as pictorial representations to support their mental and written methods of calculation.

By the end of Year 6, children should be equipped with efficient mental and written calculation methods, which they use fluently. Decisions about when to progress should always be based on the security of pupils' understanding and their readiness to move ahead to the next stage. At whatever stage in their learning, and with whatever written method is being used, children's strategies must still be underpinned by a secure understanding and knowledge of number facts that can be recalled fluently with flexibility.

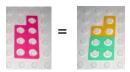
When children leave Purley Primary School our overall aim is that they:

- Are able to recall number facts with fluency having developed conceptual understanding through being able to visualise key ideas through experience with practical equipment and visual representations;
- Make use of diagrams and jottings to help record / reason through stages of thinking when using mental methods that generate more information than can be kept in their heads;
- Have an efficient, reliable, written method of calculation for each number operation (+ x ÷) that they can apply with confidence when undertaking calculations that they cannot carry out mentally;
- Are able to make connections between all four number operations, understanding how they relate to one another, as well as how the rules and laws of arithmetic can be applied.
- Have a solid understanding of the language and vocabulary used in mathematics
- Have a variety of ways to represent mathematical steps visually
- Have effective skills to decide if an answer makes sense

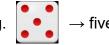
#### From Early Years to Year 1:

There are fundamental concepts that it is important for children to develop an early understanding of as building blocks to future learning in maths, including that linked to calculation. A selection of the skills include:

- Ordinality 'the ordering of numbers in relation to one another' e.g. (1, 2, 3, 4, 5...)
- Equality 'seven is the same total as four add three' e.g.



- Subitising – 'instantly recognising the number of objects in a small group, without counting them' – e.g.



- One-to-one correspondence – e.g.



- Conservation of number – 'recognising that a value of objects are the same, even if they are laid out differently' – e.g.



- aro.
- Concept of zero

$$3 + 0 = 3$$

Counting on and back from any number – e.g. 'five add three more totals eight'



'ten take away three totals seven'



Each stage/step in teaching is split into 5 columns:

**Counting** - the objective from the National Curriculum

**Mental maths strategies and linked concepts** - mental maths strategies that could be used in the stage and ideas of how they link across other parts of maths

Rapid recall - strategies that can be used in the stage that need to be practised and learnt by recall

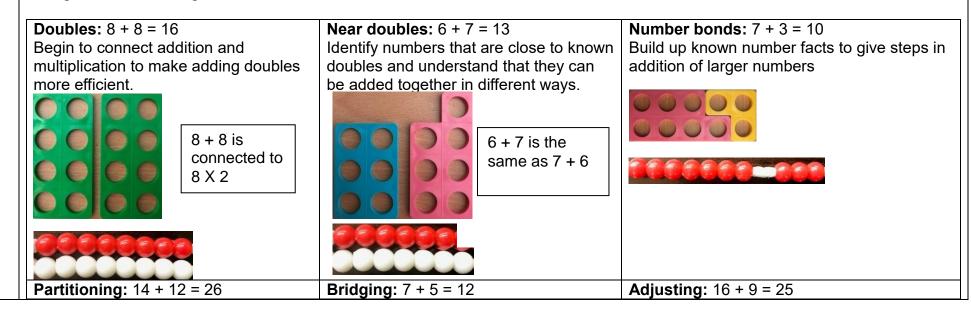
Written calculation - formal written methods

and appropriate models images to support conceptual understanding - how equipment is used to support written methods

#### Mental calculation strategies for addition and subtraction:

The ability to calculate mentally forms the basis of all methods of calculation and is a skill that has to be kept up through all stages of learning. A good knowledge and 'feel' for numbers, happens through structured practice and progression in practical math's experiences alongside visual representations.

The following strategies allow children different ways to arrange numbers in their heads and to build up skills that will be used throughout their learning.



Being able to split numbers into tens, Being able to break down a number into Being able to use numbers that are easier to ones etc and use this when adding. smaller parts to aid in adding add and know how to adjust these numbers particularly used with number bonds. after adding. To begin: 16 + 10 = 26Then: 26 - 1 = 25To begin: 7 + 3 = 10Then: 10 + 2 = 1211 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 Finding the difference: 10 - 6 = 4**Reordering:** 8 + 7 + 2 = 17Understanding that the difference can Being able to calculate numbers in a be represented as what is missing or different order. what can be added to make the total. To begin: 8 + 2 = 10Then: 10 + 7 = 17David has 10 sweets, whilst Chloe has six sweets. How many more does David have than Chloe?

	strategies & linked concepts			models/images to support conceptual standing
Count in ones to and across 100 forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten using a counting stick set up as a number track.	Explicitly teach every mental maths strategy detailed above. Pupils use apparatus to explore addition as the inverse of subtraction.	Rapid recall of all pairs of numbers totalling numbers up to 20. Use structured apparatus – i.e. Numicon, tens frames, abaci, etc.	<ul> <li>Teachers model how to line up counters/objects on a number track before counting on. This is a precursor to use of a fully numbered number-line.</li> <li>Children develop a mental picture of the number system for use with calculation. A range of key models and images support this, alongside practical equipment.</li> <li>Whole / part-whole model:         <ul> <li>The concept of a whole / part-whole model is introduced.</li> </ul> </li> </ul>	'Four add one more is the same as five'  Tens frame  Bar model  Cherry model
Continue practising above skills. Count in steps of 2, 3 and 5 forwards and	Explicitly teach every mental maths strategy detailed above. Round numbers to the nearest 10, for example,	Recall addition facts for all numbers to 20.	Counting on from the largest number:  • Children begin to use number lines to support their own calculations, initially counting on from the largest number in	Number line with all numbers labelled  0 1 2 3 4 5 6 7 8 9 10 11 12  18 + 5  10 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 +
	to and across 100 forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten using a counting stick set up as a number track.  Continue practising above skills. Count in steps of 2, 3 and 5	to and across 100 forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten using a counting stick set up as a number track.  Continue practising above skills. Count in steps of 2, 3 and 5  Every mental maths strategy detailed above. Pupils use apparatus to explore addition as the inverse of subtraction.  Four add one is the same as five?  Explicitly teach every mental maths strategy detailed above. Round numbers to the nearest	to and across 100 forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten using a counting stick set up as a number track.  Continue practising above skills. Count in steps of 2, 3 and 5  Every mental maths strategy detailed above. Pupils use apparatus to explore addition as the inverse of subtraction. Use structured apparatus – i.e. Numicon, tens frames, abaci, etc.  Explicitly teach every mental maths strategy detailed above. Round numbers to 20.	to and across 100 forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten using a counting stick set up as a number track.  Continue practising above skills. Count in steps of 2, 3 and 5  Continue practising and 5  Of all pairs of numbers to tatiling numbers to tatiling numbers to tataling numbers to tataling numbers to apparatus to explore addition as the inverse of subtraction.  Use structured apparatus – i.e.  Numicon, tens frames, abaci, etc.  Continue practising addition facts for all numbers to 20.  Continue practising above skills.  Continue practising above skills.  Continue practising above skills.  Count in strategy detailed above.  Continue practising above skills.  Count in strategy detailed above.  Continue practising above skills.  Continue practising above skills.  Continue practising and the inverse of subtraction.  Summers to 20.  Continue practising and the inverse of subtraction.  Summers to 20.  Continue practising and the inverse of subtraction.  Summers to 20.  Continue practising and the inverse of a fully numbers to apparatus – i.e.  Collidren develop a mental pricture of the number system for use with calculation. A range of key models and images support this, alongside practical equipment.  Continue practical equipment.  Continue practical above.  Summers to 20.  Continue practical equipment.  Continue practical equipment practical eq

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	backwards to and from zero using a counting stick set up as a number line. Count in tens from any number – link to coins in a piggy bank as well as a number square.	by illustrating on a number line that is drawn on a folded strip of paper.		ones before beginning to work more efficiently.  Reordering calculations to apply use of mental maths strategies:  • Children reorder 'strings' of numbers to apply their understanding of mental maths strategies, including doubles and number bonds, e.g. 6 + 7 + 4 reordered to 6 + 4 = 10 and then 10 + 7 = 17. Jottings are used to help keep track of thinking.	Questions such as: 'How might I rearrange these to find the total?' are asked.
				<ul> <li>Whole / part-whole model:</li> <li>The concept of a whole / part-whole model is reinforced and extended.</li> </ul>	Bar model Cherry model
Stage 3:	Continue practising above skills. Count forward and backwards from 0 in multiples of 4, 8, 50 and 100. Count on 10 or 100 from any two-digit number. Count up and down in tenths. Link to	Reinforce partitioning and bridging through multiples of 10, plus adjusting when adding 11 or 9. Use structured apparatus to understand that subtraction undoes addition and link with inverse number operations.	Connect pairs totalling ten to pairs of multiples of 10 totalling 100.  Use 10ps in tens frame. Recall pairs of two-digit	<ul> <li>Teachers model how numbers can be partitioned into tens and ones, including different ways, e.g. 36 = 30 + 6         36 = 20 + 10 + 6</li> <li>Add numbers using structured apparatus to support understanding of place value.</li> <li>Make connections between partitioning both numbers using structured apparatus and partition the second number only using a number line.</li> </ul>	Add

Stage 4: Continue practising previous skills. Count forwards and backwards from 0 in multiples of 6, 7, 9, 25 and 1000 using counting sticks, number lines, number squares, etc. Count up and down in tenths, and simple fractions using models and images, plus Dienes / pl		a counting stick as before, whilst deriving number facts.		numbers with a total of 100, i.e. 32 +? = 100.	This is an empty number line that helps record the steps on the way to calculating the total.	By partitioning and recombining  30+ 40 = 70  5 + 7 = 12  70 + 12 = 82  35 + 47  +30  +3  +3  +2  47  77  80  82
pixie Dielies	Stage 4:	practising previous skills. Count forwards and backwards from 0 in multiples of 6, 7, 9, 25 and 1000 using counting sticks, number lines, number squares, etc. Count up and down in tenths, hundredths and simple fractions using models and images,	through 60 for time, i.e. 70 minutes = 1 hour and 10 minutes. Rounding any number to the nearest 10, 100 or 1000. Rounding numbers with one decimal place to nearest whole number. Explore inverse as a way to derive new facts and to check accuracy of	Use known facts and place value to derive new ones, i.e. 'If I know 8 + 3 = 11, I also know 0.8 + 0.3 = 1.1 and 8/100 + 3/100 = 11/100.' Sums and differences of pairs of multiples of 10, 100 or 1000. Addition doubles of numbers to	<ul> <li>Written recording should follow teacher modelling around the size of numbers and place value using a variety of concrete/pictorial materials, e.g. Numicon shapes, Dienes and place-value cards.</li> <li>As children move towards using a columnar method, links continue to be made with earlier models and images,</li> </ul>	2.55 + 123 2.00 + 30 + 5 + 100 + 20 + 3  1.00 + 30 + 5 + 100 + 20 + 3  2.55 + 123 2.00 + 30 + 5 + 1.00 + 20 + 3  1.5  DO's  1.5  1.5  1.5  1.5  1.5  1.5  1.5  1.

	equipment and a counting stick.		Pairs of fractions totalling one.		It is important that empty number lines are kept as well as using more formal written calculation methods.  Counting on more efficiently:  34 44 54 57
Stage 5:	Count forwards and backwards in steps of powers of 10 for any given number up to one million. Continue to count forwards and backwards in simple fractions. Count forward and backwards in	Use apparatus and knowledge of place value to add decimals, i.e. $3.4 + 2.5 = 5 + 0.9$ Reorder increasingly complex calculations, i.e. $1.7 + 2.8 + 0.3 = 1.7 + 0.3 + 2.8$ Compensating – i.e. $405 + 399$	Continue to practice previous stage and make links between known facts and addition pairs for fractions, percentages and decimals Doubles and halves of decimals, i.e. half of	<ul> <li>Expanded vertical method, leading to columnar addition:         <ul> <li>Teachers model a column method that records and explains partial mental methods.</li> </ul> </li> <li>There remains an emphasis on the language of calculation, e.g. 'Forty plus seventy equals one-hundred and ten.' 'Seven add six equals thirteen.' before recombining numbers. Teachers also model the language of: 'Four tens add seven tens total eleven tens or 110.'</li> </ul>	Informal columnar:  Adding the hundreds first: 471  + 356  700  120

	appropriate decimals and percentages.	→ add 400 and then subtract one.	5.6, double 3.4. Sums and differences of decimals, i.e. 6.5 + 2.7	Teachers similarly advance to model the addition of two 3-digit numbers with the expectation that as children's knowledge of place value is secured, they become ready to approach a formal compact method.
Stage 6:	Continue to practice previous skills. Count forwards and backwards in simple fractions, decimals and percentages.	Bridging through decimals, i.e. $0.8 + 0.35 = 0.8 + 0.2 + 0.15$ using empty number lines. Partitioning using near doubles, i.e. $2.5 + 2.6 = 5 + 0.1$ Reorder decimals, i.e. $4.7 + 5.6 - 0.7$ as $4.7 - 0.7 + 5.6 = 4 + 5.6$ .	Using children's confident recalling of basic facts to 20/100 and deriving facts using place value, make links between decimals, fractions and percentages. i.e. 1 + 19 10 + 190 100 + 1900 Question: What do you notice?	Columnar addition (formal written method):  The concept of exchange is reinforced through continued use of equipment.  Teachers model:  1. "I have two tens and five ones, which need adding to four tens and seven ones."  2. "I add five ones to seven ones, which gives me twelve ones."  3. "I exchange ten of my twelve ones for a ten counter."  4. "I add my three tens and four tens to make seven tens."  "Altogether, I have seven tens and two ones."  Teachers similarly advance to model the addition of two 3-digit numbers and then go beyond.  Pupils to be encouraged to consider mental strategies first.  Formal columnar – using an example with smaller value numbers:  25  +47  -2

	587 + 475 1062	

#### **Subtraction:**

	Counting	Mental strategies	Rapid Recall	Written calculation and conceptual understand	d appropriate models and images to support
Stage 1:	Count in ones to and across 100, forwards and backwards starting from 0, 1 and other numbers. Count in multiples of two, five and ten.	Explicitly teach every mental maths strategy detailed above. Pupils use apparatus to explore addition as the inverse of subtraction:  'One less than five is four'	Rapid recall of subtraction facts for numbers up to 10. Use structured apparatus, i.e. Numicon, tens frames, abaci etc.	Subtraction as taking away from a group:  • Teachers model how to remove counters/objects and count back on a number track. This is a precursor to use of a fully numbered number-line.  Whole / part-whole model:  • The concept of a whole / part-whole model is introduced.	'Five minus two totals three' 'Six take away two leaves four'  'One less than six is five'  Tens frame  Bar model  Cherry model
Stage 2:	Continue practising above skills. Count in steps of 2, 3 and 5,	Explicitly teach every mental maths strategy detailed above.	Recall subtraction (and addition) facts for all	Taking away:  • Children begin to use number lines to support their own calculations,	Number line with all numbers labelled  0 1 2 3 4 5 6 7 8 9 10 11 12

Stage	forwards and backwards to and from zero. Count in tens from any number – link to coins in a piggy bank as well as a number square.  Continue	Reinforce	numbers to 20.	initially counting back in ones before beginning to work more efficiently.  Finding the difference:  • Teachers model how to find the difference when two numbers are relatively 'close together.'  Taking away:	13 – 5 = 8  1
3:	practising above skills. Count from 0 in multiples of 4, 8, 50 and 100. Count on and back by 10 or 100 from any two digit number. Link to counting stick counting forwards and backwards flexibly. Count up and down in	partitioning and bridging through multiples of 10, plus adjusting when subtracting 11 or 9. Use structured apparatus to understand that subtraction undoes addition and link with inverse number operations.	subtractions from ten to subtractions from multiples of 10 totalling 100.  Use 10ps in tens frame. Subtract two digit numbers from 100 i.e. ? = 100 - 78	When teaching children about reduction, highlight the importance of only partitioning one number.	linked with a horizontal expanded written number sentence: $167 - 24 = 143$ $20   4$ In either order $To begin: 167 - 20 = 147$ $Then: 147 - 4 = 143$ $100 + 60 + 7$ $\frac{20 + 4}{0 + 40 + 3}$

	tenths – linking to visual image.			Finding the difference:  • Children move on to find the difference by making number line comparisons.	Finding the difference on a number line:  Children should note that finding the difference is often the most efficient way of solving a subtraction problem when two numbers are close together. e.g. 61 – 59
Stage 4:	Continue practising of previous skills. Count forwards and backwards from 0 in multiples of 6, 7, 9, 25 and 1000 using counting sticks, number lines, number squares, etc. Count up and down in tenths, hundredths and simple fractions using models and images,	Bridging through 60 for time, i.e. 70 minutes = 1 hour and 10 minutes Rounding any number to the nearest 10, 100 or 1000. Rounding numbers with one decimal place to nearest whole number. Explore inverse as a way to derive new facts and to check accuracy of answers.	As above. Use known facts and place value to derive new ones, i.e. 'If I know 11 - 3 = 8, I also know 1.1 - 0.3 = 0.8 and 8/100 - 3/100 = 5/100.' Sums and differences of pairs of multiples of 10, 100 or 1000. Subtraction of fractions totalling 1, i.e. 1 - 0.3 = 0.7	• Subtraction by partitioning with use of manipulatives, and including transfer / exchange, linked with a horizontal expanded written calculation in preparation for a future formal column method.	363 - 147 = 216 50 13 300 + 60 + 3 - 100 + 40 + 7 200 + 10 + 6

i.e. Dienes / Pixie Dienes equipment, counting stick, ITPs.  Stage 5: Count forwards and backwards in steps of powers of 10 for any given number up to one million. Continue to count forwards and backwards in simple fractions. Count forward and backwards in appropriate	decimals, i.e. $3.8 - 2.5 = 1.3$ Reorder increasingly complex calculations, i.e. $1.7 - 0.5 - 0.7 = 1.7 - 0.7 - 0.5$ .	Continue to practise previous stage and make links between known facts and addition pairs for fractions, percentages and decimals. Doubles and halves of decimals, i.e. half of	Finding the difference:  • Finding the difference continues to be highlighted where the two numbers are close together — using a number line on a strip of paper.  Column method with Dienes:  • Subtraction by partitioning with use of manipulatives, and including transfer / exchange, linked with a formal column written method.	5 1 363 - 147 - 216
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Stage	decimals and percentages.  Continue to	Bridging through	5.6, double 3.4. Sums and differences of decimals, i.e. 6.5 + 2.7 Using	Column method with	Punils to be encouraged to consider mental
6:	practise previous skills. Count forwards and backwards in simple fractions, decimals and percentages.	decimals, i.e. 1.5 – 0.8 = 1.5 – 0.5 then – 0.3 using empty number line.	children's confident recalling of basic facts to 20/100 and using place value, make links between decimals, fractions and percentages. 19 – 1 = 190 – 10 = 1.9 – 0.1 = Question: What do you notice?	place value counters:         • The concept of transfer / exchange is continued through use of manipulatives.         • Teachers model:             1. "I have seven tens and two ones. I need to subtract four tens and seven ones."             2. "At the moment, I cannot subtract seven ones from two ones, so I need to transfer one ten to become ten ones."	Pupils to be encouraged to consider mental strategies first.  Formal columnar – using an example with smaller value numbers to exemplify:  72 -47 -47 -5 -47 -5 -68 -68 -68 -68 -68 -68 -68 -68 -68 -68

<del>_</del>
3. "Now I can
take away
seven ones
from twelve
ones, so that
I have fives
ones left."
4. "I can now
subtract four
tens from six
tens, which
leaves me
with two
tens."
5. "I recombine
two tens and
fives ones to
understand
that I am left
with twenty-
five."

#### **Multiplication:**

#### Mental calculation strategies for multiplication and division:

#### Doubling and halving:

Double six is 12... Double five is ten...



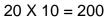
Double 16 can be calculated by working out...

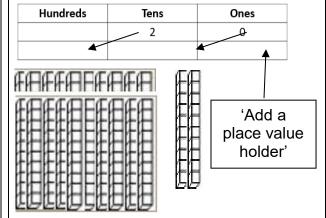
Double ten  $\rightarrow$  20 Double six  $\rightarrow$  12



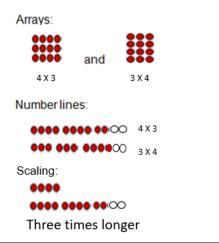
With links to finding four-times a given value and finding a quarter of a value.

# Multiplying and dividing by multiples of ten:

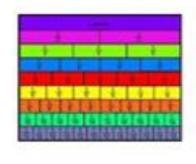




## Knowing multiplication and division facts to 12 X 12:

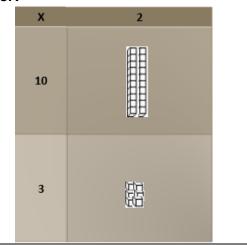


# Identifying fractions, decimals and percentages:





### Multiplying a teen number by one-digit number:



Milk the maths...



...by allowing children to make connections between number facts.

Counting

**Mental strategies** 

Rapid recall

Written calculation and appropriate models and images to support conceptual understanding

Stage 1:	Count forwards and backwards in 2s, 5s and 10s	Doubling up to six and then ten whilst using related models and images.	Derive/recall doubles up to five and derive/recall halves up to ten.	Developing early conceptual understanding of multiplication (grouping):	Use objects, pictorial representations and arrays to show the concept of multiplication:  Early bar model ?
Stage 2:	Count forwards and backwards in 2s, 3s, 5s and 10s from zero.	Begin to understand and use inverse number operations:  10 2 5  Stories are used alongside a triad to help children understand links between number operations, e.g. "There are five pencils in two packs, which means that there are ten pencils altogether."  Doubling is reinforced using a whole/part-whole model:	Derive/recall doubles up to ten and derive/recall halves up to twenty.  Recall & use multiplication facts for the 2X, 5X and 10X-tables.  Learn what happens when a number is multiplied by zero or one.	Understanding multiplication as repeated addition:  Investigate multiplication as repeated addition, so that the law of cummutativity is understood.  Whilst arrays are also modelled explicitly at this stage, it is important to note that they will continue to be a key model at later stages,	Arrays:  5 X 3  and  3 X 5  with both array and repeated addition images.  Repeated addition on the number line linked with manipulatives:  6 X 4 = 24  So: 'Six multiplied by four'or 'Six taken four times.'

Stage 3:	Counting forwards	Use doubling to make connections between the 2X, 4X		alongside more formal methods of calculation.  Relate multiplying a 2-digit by 1-digit	Children use an empty number line to group efficiently:
	and backwards in 2s, 3s, 4s, 5s, 8s and 10s from zero.  Count up and down in tenths.	and 8X-tables.  Understand that multiplication can be undertaken by partitioning numbers, e.g. 12 X 4 = 10 X 4 + 2 X 4  Introduce the structure of scaling: e.g. Find a ribbon that is 4 times as long as the blue ribbon  2cm 8cm	multiplication facts for the 2X, 3X, 4X, 5X, 8X and 10X tables.	number using repeated addition and arrays to represent:	4 X 12 = 48  4 X 10 = 40  4 X 2 = 8  3 X 13 = 39  X  10  3  7 X 13 = 91
Stage 4:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 7s, 8s, 10s, 25s and 1000s from zero.  Count up and down in	Derive factor pairs of numbers using models and images, e.g. Cuisenaire 1 and 12 2 and 6 3 and 4	Recall & use multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 3 or 2-digit by 1- digit number with arrays towards using long/short multiplication:	Relate multiplying a 3/2-digit by 1-digit number, whilst refining the written notation used.  114 X 2 = 228  X 100 10 4

	tenths and hundredths.	Use reordering to multiply three numbers.  Children learn about the associative law: (9 X 5) X 10 = (10 X 5) X 9			114 X 2 =  100 X 2 = 200 10 X 2 = 20 4 X 2 = 8 = 228  At this stage, the <b>non-statutory</b> guidance in the National Curriculum suggests teaching short multiplication; however, the team feel that an expanded form of calculation (as set out above) is be a better lead into long/short multiplication.
Stage 5:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 25s and 1000s from zero.	Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 4/3/2-digit by 1/2-digit number with grid to using long multiplication:	10 8  10 100 80  3 30 24  18 X13  24 30 80 100 234

Stage 6:	Consolidate all previous counting, including forwards and backwards in fractions.	Perform mental calculations, including with mixed numbers and operations.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Relate multiplying a 4/3/2-digit by 1/2-digit number with grid to using short multiplication:	10 100 80 3 30 24 18 X13 54 2 180 234
					Once children have fully grasped the concept of multiplication alongside equipment and an expanded written method, they will be well-placed to progress towards a more compact written method.

#### **Division:**

	Counting	Mental strategies	Rapid recall	Written calculation and appropriate models and images to				
Stage 1:	Count forwards and backwards in 2s, 5s and 10s	Doubling up to six and then ten whilst using related models and images.	Derive/recall doubles up to five and derive/recall halves up to ten.	support conceptual Developing early conceptual understanding of division as grouping and sharing:	• • • •			
Stage 2:	Count forwards and backwards in 2s, 3s, 5s and 10s from zero.	Begin to understand and use inverse number operations.	Derive/recall doubles up to ten and derive/recall halves up to twenty.  Recall and use multiplication facts for the	Understanding division as repeated subtraction:  • Investigate division as repeated subtraction.  • Through teacher modelling,	Number lines: $12 \div 3 = 4$ $15 \div 5 = 3$			

		Stories are used alongside a triad to help children understand links between number operations, e.g. "15 children are asked to get into three groups and find out that there are five people in each group."	2X, 5X and 10X-tables.	children need to know that division is not commutative.	0 5 10 15  Early bar model
Stage 3:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 8s and 10s from zero.	Use doubling to make connections between the 2X, 4X and 8X-tables.  Understand that multiplication can be undertaken by partitioning numbers, e.g. 12 X 4 = 10 X 4 + 2 X 4  Introduce the structure of scaling: e.g. Find a ribbon that is 4 times as long as the blue ribbon.	Recall & use multiplication facts for the 2X, 3X, 4X, 5X, 8X and 10X tables.	Dividing a 2-digit by 1-digit number, representing this efficiently on a number line:	Children use an empty number line to chunk efficiently.  96 ÷ 6 = 16  6 x 6 = 36  10 x 6 = 60  0  36  96  Conceptual understanding can be provided through use of a bead string to highlight the chunks.
Stage 4:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 7s, 8s, 10s, 25s and 1000s from zero.	Derive factor pairs of numbers using models and images, e.g. Cuisenaire.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Dividing a 3 or 2-digit by 1-digit number, representing this efficiently on a number line, also in relation to long division:  • At this stage, remainders may be present in a	Children use an empty number line to chunk efficiently.  224 ÷ 8 = 28  8 x 8 = 64  20 x 8 = 160  0  64  224  28  8  224  - 160 (8 X 20)  20 X 8 = 160

				practical context.	64or 64 - <u>64</u> (8 X 8) 8 X 8 = <u>64</u>
Stage 5:	Counting forwards and backwards in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 25s and 1000s from zero.	Identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Dividing a 4/3/2-digit by 1-digit number, in relation to long division:  • By this stage, there is a statutory requirement that children can use a formal written calculation method, such as long division.  • Short division may begin to be taught alongside long division, but still with use of visual representations	Remainders should be interpreted in the following ways when long division is used:  • as whole numbers  • as fractions  • through rounding in an appropriate way to the context  Long division:  415 ÷ 9 = 46 and 1/9  46 and 1/9  9 415  40 X 9 = 360  55  6 X 9 = 54  1
Stage 6:	Consolidate all previous counting, including forwards and backwards in fractions.	Perform mental calculations, including with mixed numbers and different number operations.	Recall & use multiplication facts for all times-tables up to 12 X 12.	Dividing a 4/3/2-	Remainders should be interpreted in the following way when short division is used:  • through rounding in an appropriate way to the context  Long division:  432 ÷ 15 = 28 4/5   28  15   432  20 X 15 = 300

	can use formal written calculation methods, including long and short division.  Use of visual representations – like the ones opposite	132 8 X 15 = 120 12 12 = 4 5 Answer: 28 $\frac{4}{5}$ Short division: 138 ÷ 6 = 23		Tens	Ones
	– remain important.	23 6 \( \frac{23}{13} \) 8	23 ① ① ① ① ② ① ① ② ③ ② ② ② ② ② ③ ② ③ ③ ③ ③ ③ ③ ③ ③ ③ ③ ③ ③		23
		Key language: 'How many growthere in one-hu 'How many growthirteen tens?' 'How many groweighteen?'	ndred?' ups of s	six tens are	e there in